

SIDDHARTH INSTITUTE OF ENGINEERING & TECHNOLOGY:: PUTTUR (AUTONOMOUS) B. Tech I Year II Semester Regular Examinations October-2020 DIFFERENTIAL EQUATIONS AND VECTOR CALCULUS

(Common to CE, EEE, ME, ECE & AGE)

Time: 3 hours

Max. Marks: 60 M

6M

(Answer all Five Units $5 \times 12 = 60$ Marks) UNIT-I

1 a Solve the D.E
$$(y^2 - 2xy)dx + (2xy - x^2)dy = 0$$
 6M

b Solve the Bernoulli's D.E
$$x \frac{d y}{d x} + y = x^3 y^6$$
 6M

2 a Solve
$$(D^2 - 4D + 3)y = 4e^{3x}$$
 given $y(0) = -1$, $y'(0) = 3$.

b Solve
$$(D^2 + 4D + 3) v = e^{-x} \sin x + x$$
 6M

UNIT-II

a Solve
$$(D^2 - 2D)y = e^x \sin x$$
 by method of variation of parameters. 6M
b Solve $\frac{d^2y}{dx^2} + \frac{1}{x}\frac{dy}{dx} = \frac{12 \log x}{x^2}$ 6M

4 An uncharged condenser of capacity is charged applying an e.m. f $E \cdot \sin\left(\frac{t}{\sqrt{LC}}\right)$ through leads of self-inductance L and negligible resistance. Prove that at time 't', **12M** the charge on one of the plates is $\frac{EC}{2} \left[\sin\left(\frac{t}{\sqrt{LC}}\right) - \frac{t}{\sqrt{LC}} \cos\left(\frac{t}{\sqrt{LC}}\right) \right]$.

UNIT-III

5 a Form the Partial Differential Equation by eliminating the constants a,b from $z = a \cdot \log \left[\frac{b(y-1)}{(1-x)} \right].$ 6M

b Form the Partial Differential Equation by eliminating the arbitrary functions f from $x y z = f(x^2 + y^2 + z^2).$ 6M

OR

6 a Solve p(1+q) = qzb Solve by the method of separation of variables $u_x - 4u_y = 0$, where $u(0, y) = 8e^{-3y}$ 6M

R19

UNIT-IV a Find the directional derivative of $2xy + z^2 \operatorname{at}(1, -1, 3)$ in the direction of $\vec{i} + 2\vec{j} + 3\vec{k}$. 7 **6M b** Find a, if $\overline{f} = y(ax^2 + z)\overline{i} + x(y^2 - z^2)\overline{j} + 2xy(z - xy)\overline{k}$ is solenoidal. 6M

$$\mathbf{OR}$$

8 a Find
$$\nabla \times (\nabla \times \overline{f})$$
, if $\overline{f} = (x^2 y)\overline{i} - (2xz)\overline{j} + (2yz)\overline{k}$ 6M

b Prove that
$$\nabla \cdot (\overline{f} \times \overline{g}) = \overline{g} \cdot (\nabla \times \overline{f}) - \overline{f} \cdot (\nabla \times \overline{g})$$
 6M

9 a If
$$\overline{F} = (5xy-6x^2)\overline{i} + (2y-4x)\overline{j}$$
 then evaluate $\int_c \overline{F} \cdot d\overline{r}$ along the curve 'c' in
 xy -plane $y = x^3$ from (1,1) to (2,8).

b If $\overline{F} = 2xz\overline{i} - x\overline{j} + y^2\overline{k}$ then evaluate $\int \overline{F} \cdot dv$ where 'v' is the region bounded by **6M** the surfaces x = 0, x = 2; y = 0, y = 6; and $z = x^2$, z = 4. OR

Verify Green's theorem in a plane for $\iint (x^2 - xy^3) dx + (y^2 - 2xy) dy$ where 'c' is **12M** 10 a square with vertices (0,0), (2,0), (2,2) and (0,2).

*** END ***